

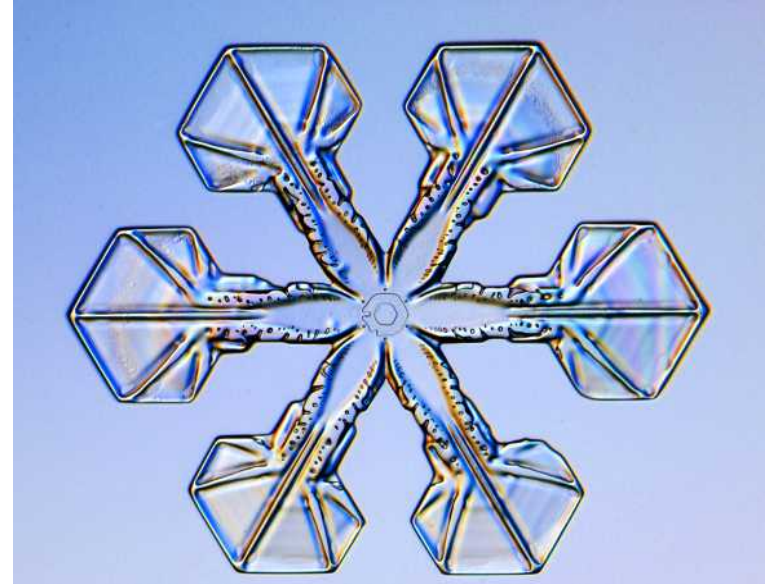
Particles, characteristic, sort



Contents of lecture

- 1. Characteristics of particles
- 2. Percolation
- 3. Number of particles in composite
- 4. Influence of particles on matrix
- 5. Curiosity of nanoparticles

Forms of snowflakes



$$d_s = 0,5 \text{ mm}$$

$$D = 1/d_s = 2 \cdot 10^5 \text{ m}^{-1}$$

Snowflake have cca 1/10 volume of sphere

Surface of snowflake is more then ten surfaces of sphere

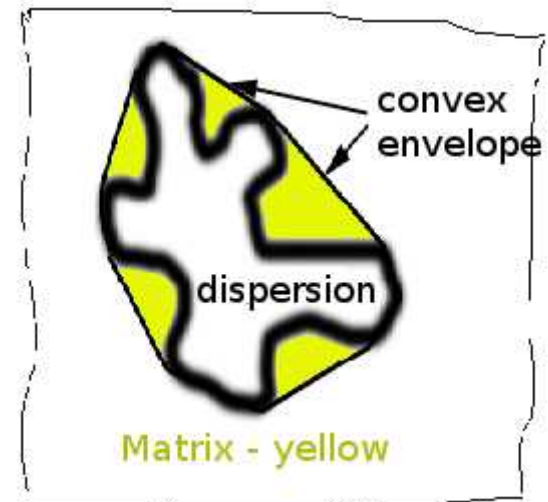
Ratio of surface to volume of snowflake $S = 10^8 \text{ m}^{-1} \text{ (m}^2/\text{m)}$

Characteristic of particle - convexity

Determines possibility of mechanical coupling of particle in matrix.

Coefficients of convexity :

- $C_1 = (\text{surface of particle}) / (\text{surface of convex envelope})$
 - exact
- $C_2 = (\text{surface of cross section of particle}) / (\text{surface of convex envelope})$
 - from cut
 - practical, not exact



Characteristic of particle - isometry

Characteristic of ability to have no significant direction (without significant orientation) - result is isotropy of composite

Coefficients of isometry :

$$\oplus F_1 = 4 * \pi * (\text{area of cross section}) / (\text{circumference of cross section})^2$$

$$\text{ball } F_1 = 4 * \pi * (\pi r^2) / (2 \pi r)^2 = 1$$

$$\text{cube } F_1 = 4 * \pi * (a^2) / (4a)^2 = \pi / 4 = 0,79$$

$$\text{long bar } F_{1k} = 4 * \pi * (\pi r^2) / (2 \pi r)^2 = 1 \dots \text{transversal}$$

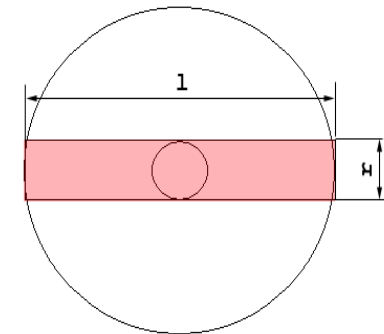
$$F_{1o} = 4 * \pi * (rl) / (2 * (l+r))^2 \approx 2 * \pi * r / l \rightarrow 0 \dots \text{axial}$$

$$\oplus F_2 = \text{radius of inner circle} / \text{radius of outer circle}$$

$$\text{ball } F_2 = 1$$

$$\text{cube } F_2 = 1 / \sqrt{2} = 0,71$$

$$\text{long bar } F_{1k} = r / r = 1 \quad F_{1o} = r / l \rightarrow 0$$



Characteristic of particle - size

- ➔ **Sieve analysis - dimension d_s** - diameter of sieve opening, into which particle sink
- only upper limit (maximum)
- ➔ **Specific surface - $S = \text{surface} / \text{mass of particle}$**
from assumption ball or cube
$$S = 6a^2 / \rho a^3 = 6/(\rho * a)$$
Equivalent diameter **$d_p = 6 / (\rho * S)$** ,
 ρ ... density, better simple **$d_p = 6 * V / F$** ,
 V ... volume and F ... surface of particle
- ➔ **Degree of dispersity $D = 1 / d \text{ (m}^{-1}\text{)}$**
- from physical chemie
Particle of ball or cube shape 1 μm great has
dispersity $D = 10^6 \text{ m}^{-1}$

Characteristic of particle - distinguishable

With optical microscope

- $d > 1 \mu\text{m}$, $D < 10^6 \text{ m}^{-1}$, particle

Scanning electron microscope

- SEM - 0,1 bis $1 \mu\text{m}$,
microparticle, $D = 10^6$ až 10^7 m^{-1}

TEM - below 100 nm,

nanoparticle, $D > 10^7 \text{ m}^{-1}$

Distance of particles regular square arrangement

Free distance between particles

$$S_{\min} = a - d, S_{\max} = a\sqrt{2} - d$$

Volume particle concentration

$$v_d = (\pi d^2/4) / a^2$$

By integration from S_{\min} till S_{\max}

we can calculate mean free distance between particles

$$S = \sqrt{(2/3)*d} / \sqrt{v_d}$$

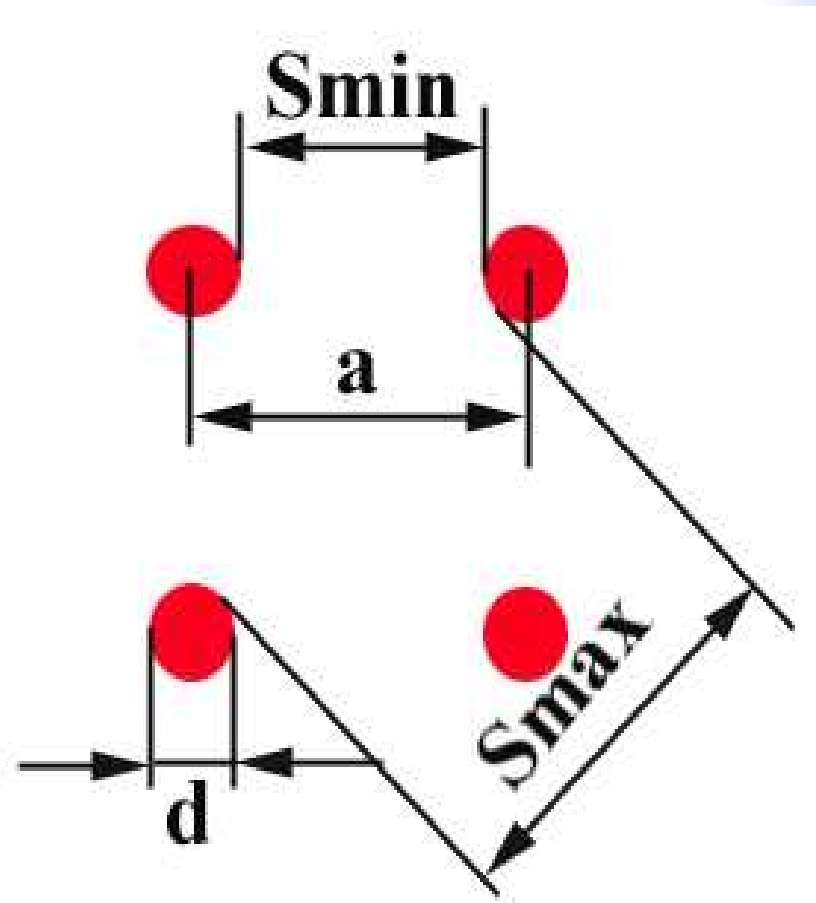
Because

$$S_{\min} = d * ((\sqrt{\pi} / (2\sqrt{v_d})) - 1),$$

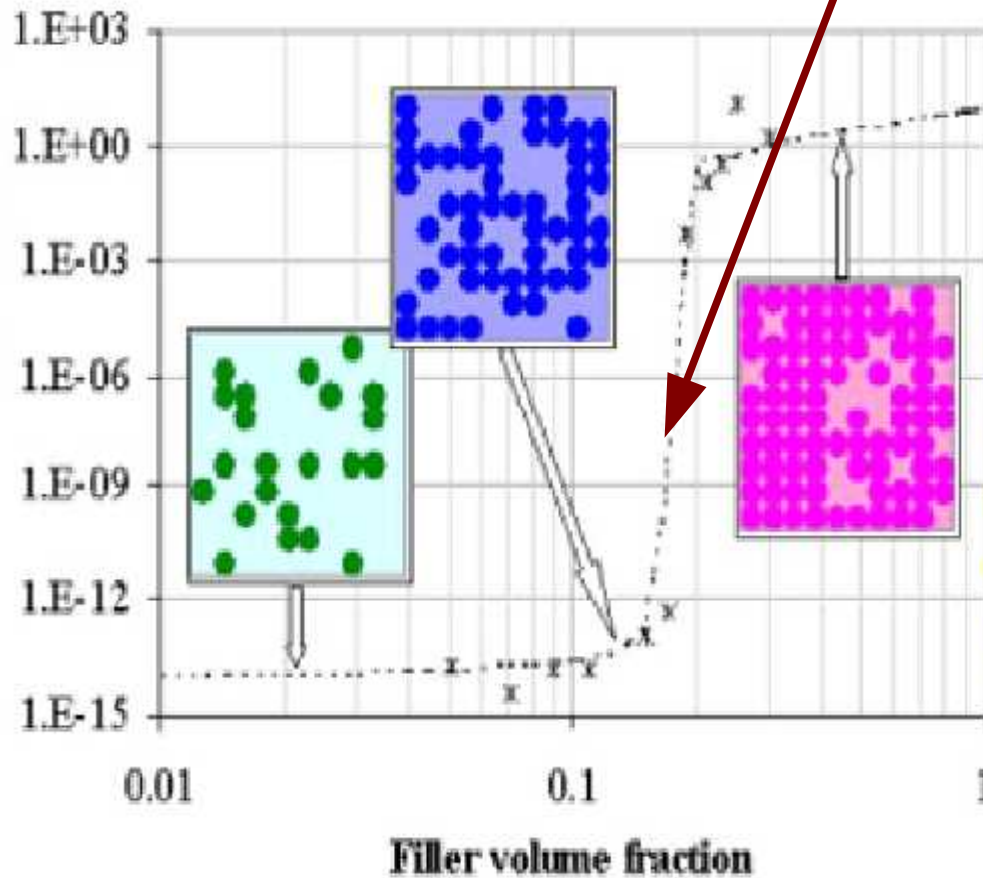
for $S_{\min} = 0$ we have

$$v_d = \pi/4 = 0,785,$$

above that concentration are all particles in contact.



Percolation limit

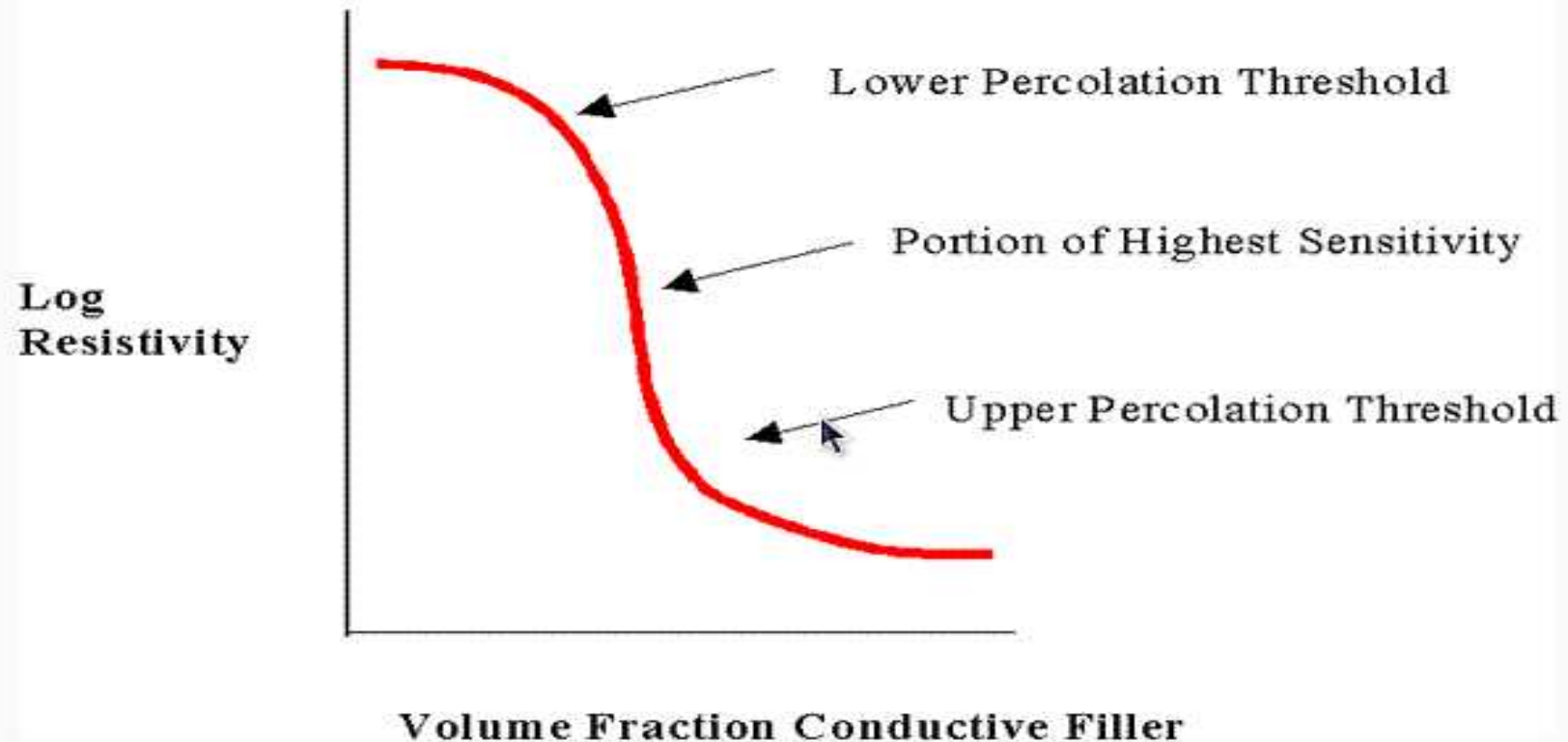


$$\sigma_c = \sigma_f (\phi_f - \phi_c)^s$$

- σ_c – conductivity of composite
- σ_f – conductivity of dispersion
- ϕ_f – concentration of dispersion
- ϕ_c – percolation coefficient
- s – percolation exponent

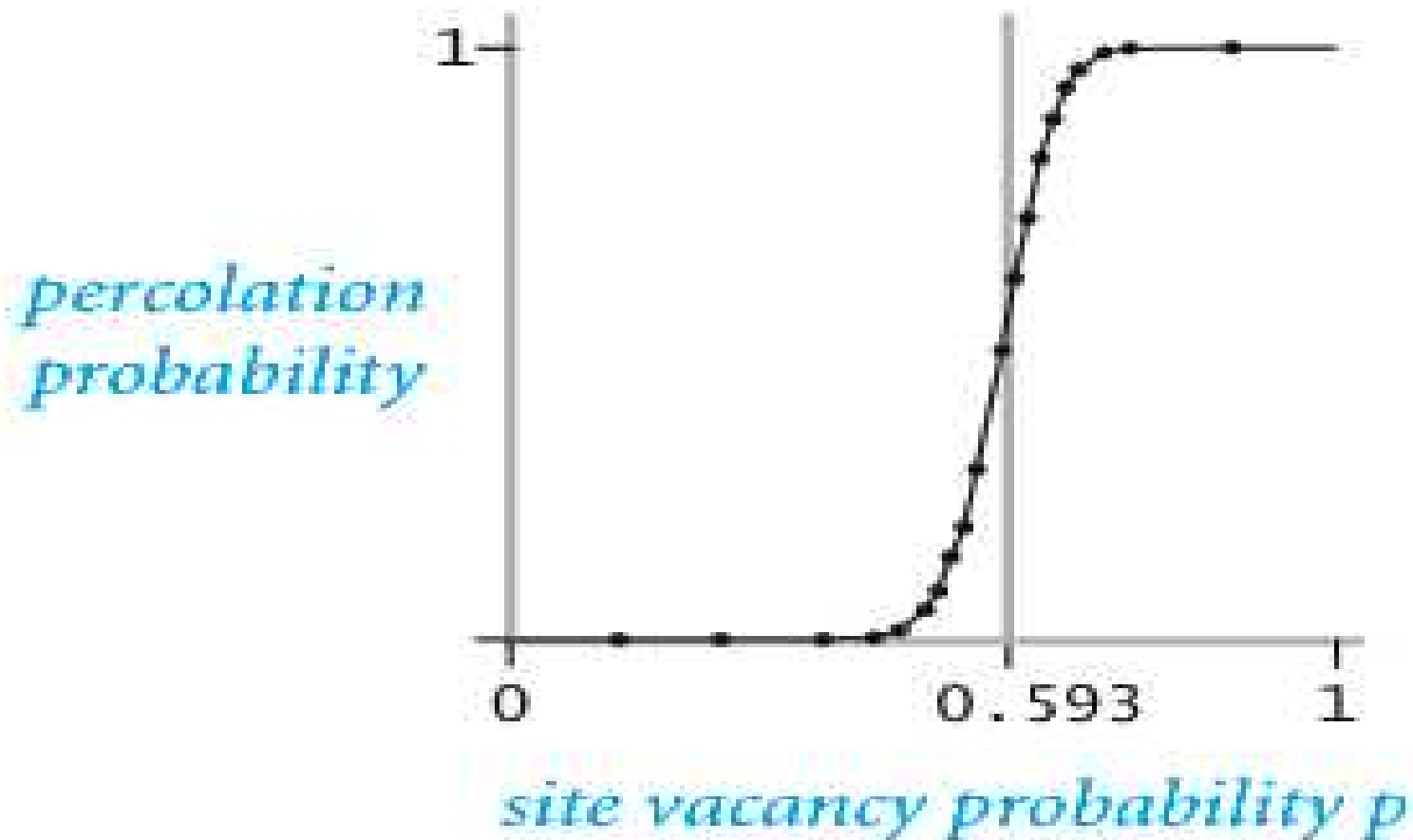
Results of electric conductivity simulation
– non-conductive matrix, conductive dispersion

Example of percolation curve



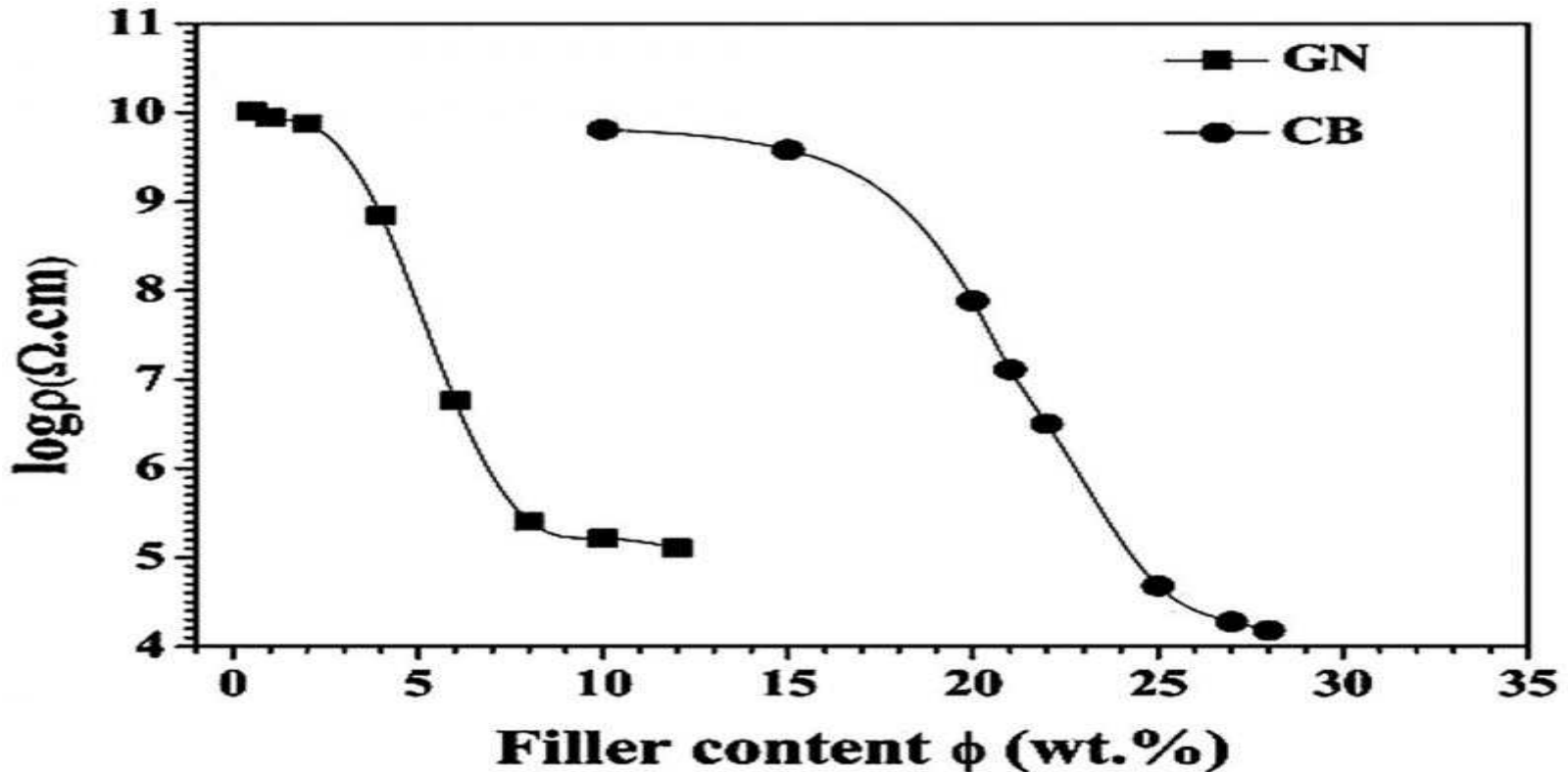
Valid for electric and thermal conductivity, hardness, by pore for gas permeability

Results of simulation



Princeton - square pore, permeability of plate

Effect of particle size



Electric resistance, matrix HDPE,
CB ... soot, GN ... graphene nanoflakes
(Guohua Chen, 2010)

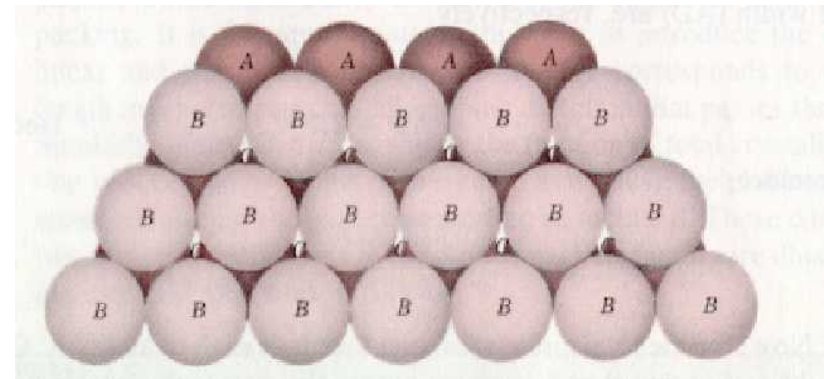
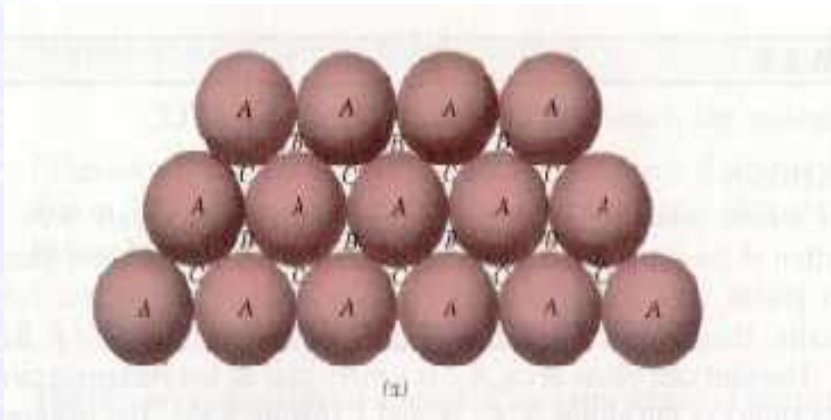
Closely packed particles

Quantity of particles – always volume %.

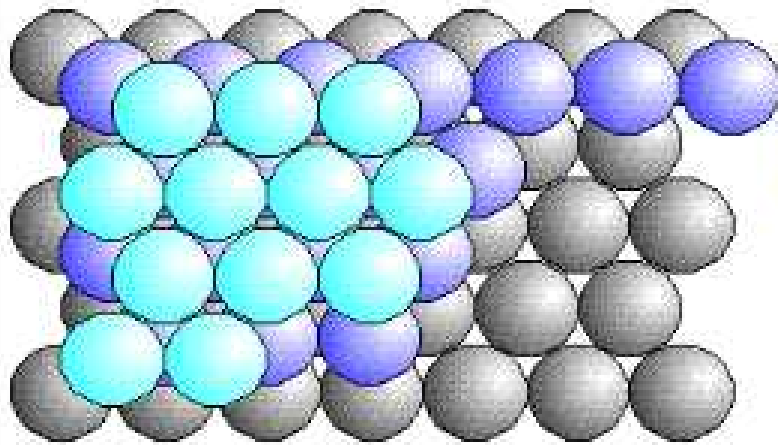
Assumption of globular (isometric) particles.

Closely packed on plain - equilaterale triangles

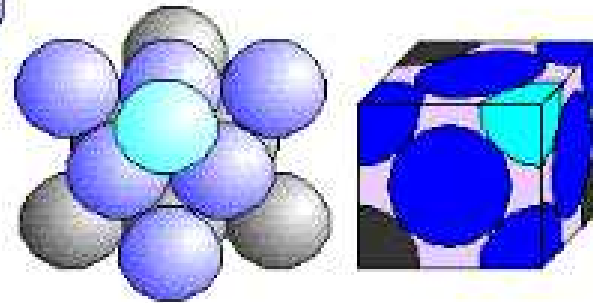
In space – the same plains sitting one on other
– from the side the same picture



Another picture on close packing



a - close packing



b - unit cell

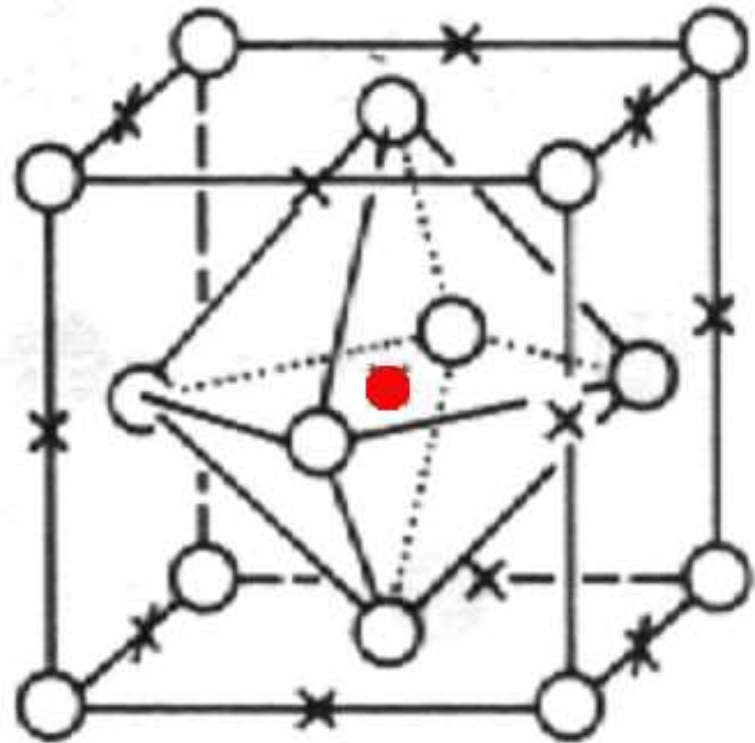
Radius of particle ... r
Diagonale of side of cube $4*r$, its edge $4*r/\sqrt{2}$
Volume of cube $64*r^3/(2*\sqrt{2})$
Inside four ball particles $4 * 4/3*\pi*r^3$

Maximale concentracion of particles

- Particles could be maximal in clouse packing
 - that is 74 % of particle dispersion a 26 % of matrix
- If is more of particles, could be leeks in matrix, that leeks are closed
- There is theoretical calculation :
 - particles are never quite perfectly arranged
 - particles have not perfect ball shape
- In practice are in composites leeks already above 55 - 60 % particles
- Quantity of matrix in composite must be above 35 až 40 volume percent, to have composite without leeks

Maximale size of leeks

Red - octaedric void in cube - maximal possible closed leek. Its radius $0,41 * r$
Also in cube with volume $64 * r^3 / (2 * \sqrt{2})$ is volume of particles $4 * 4/3 * \pi * r^3$ and volume of leeks $0,41 * 4/3 * \pi * r^3$



Connecting of leeks

By maximal shape of leeks from previous picture composite have in 100 % volume 74 % particles, 18,5 % leeks and only 7,5 % matrix.

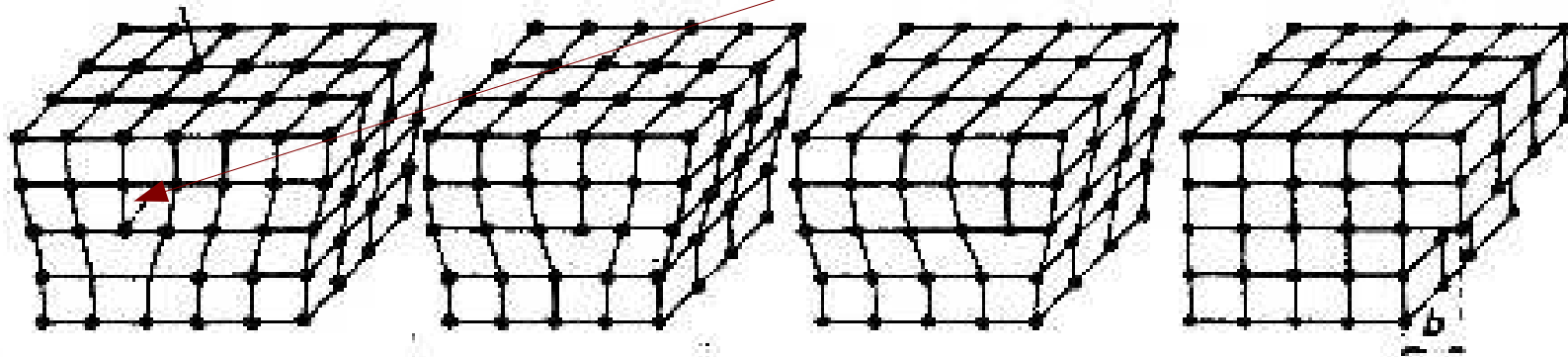
If is concentration of matrix above that quantity, leeks are closed in inner of composite.

If is concentration of matrix below that quantity, leeks begin to connect and create in composite microchannels – capillarries. Composite is becomming permeable for fluid and gas.

Again theoretical calculation - in practice are in composites leeks in microchannels already above 70 % particles.

Plastic deformation of composite

- Particles can hinder plastic deformation.
- Main cause of plastic deformation is movement of line defects - dislocations



Movement of dislocation

Strengthening due to armour

Great particles could not hinder movement of dislocation (dislocations can walk around particles), but take part of forces.

Optimum - particles above $1\ \mu\text{m}$, approximately 25 %. By greater quantity of particles - tearing of matrix.

Near particles is hydrostatic pressure.

Brittle particles are due to that pressure deformable, crack above $3 * \text{yield strength}$

By ductile particles due to that pressure decrease yield strength - they are sooner deformable.

Nanoparticles are very small for that effect.

Strengthening due to dispersion

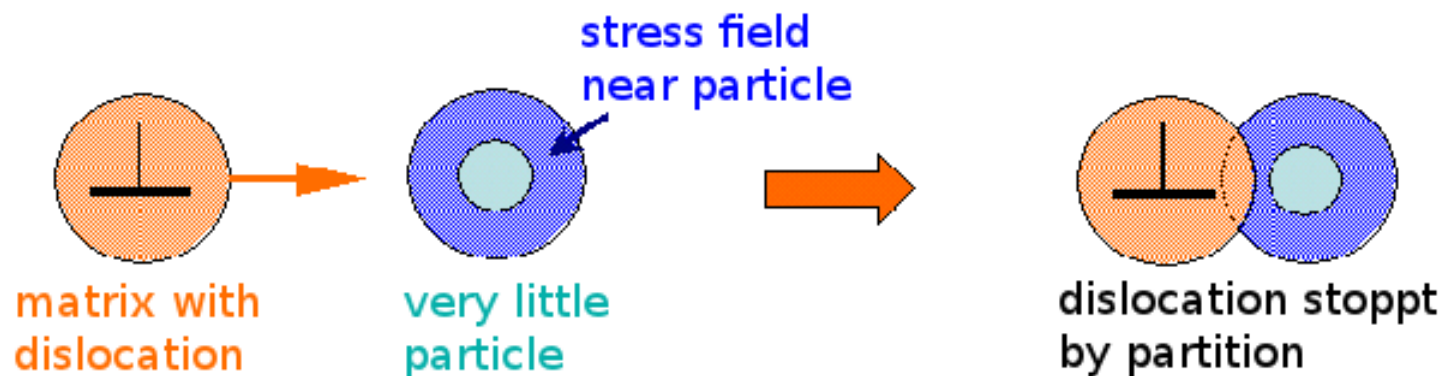
Stress necessary to movement of dislocations between micro - or nanoparticles is inverse proportional distance between particles.

Optimale distance and quantity of particles is composite with etwa 15 % nanoparticles with diameter near 100 nm.

Ultimate strength is not too increased, bud composite is very resistant to creep, bis 80 % melting point.

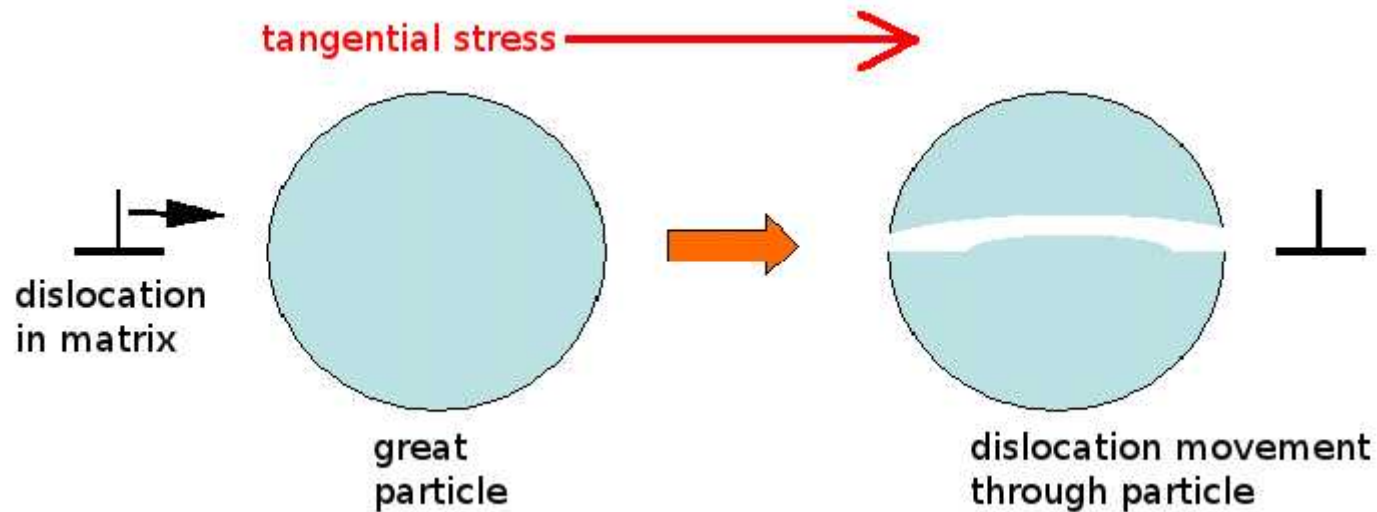
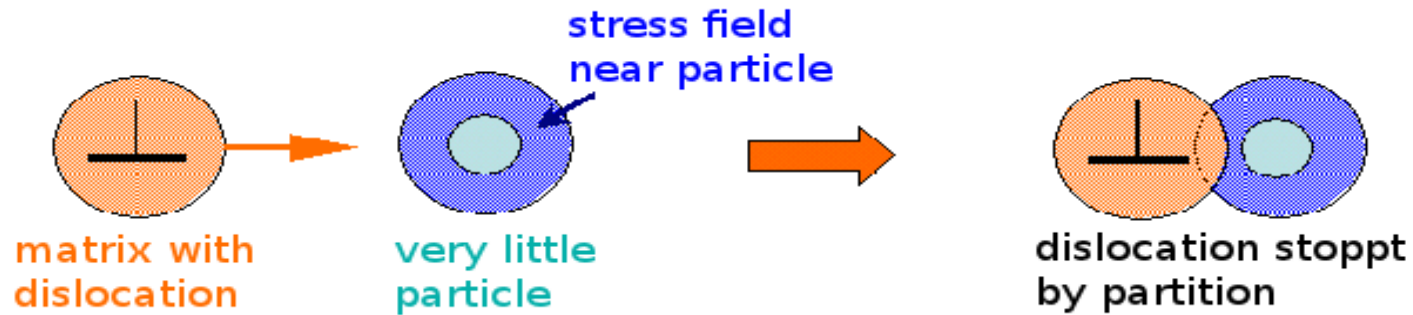
(usual metals bis 50 % melting point)

Examples : Cu - SiO₂, Fe - Al₂O₃, Ni - TiC



Comparison of strengthening

Dispersion strengthening



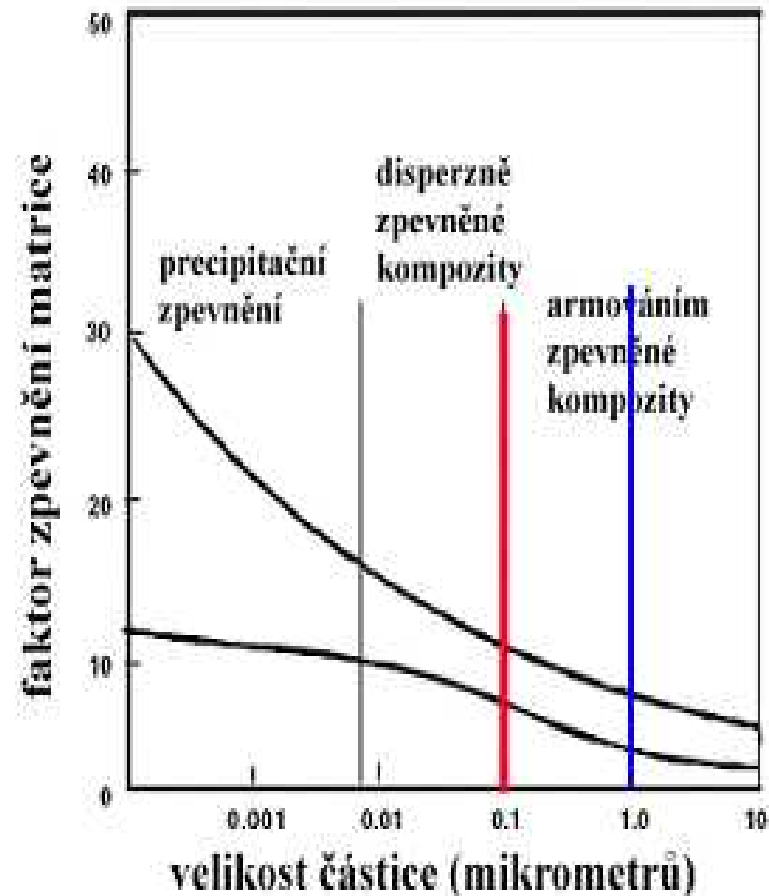
Armour strengthening

Comparison of metal hardening

Precipitation hardening - typical by metals

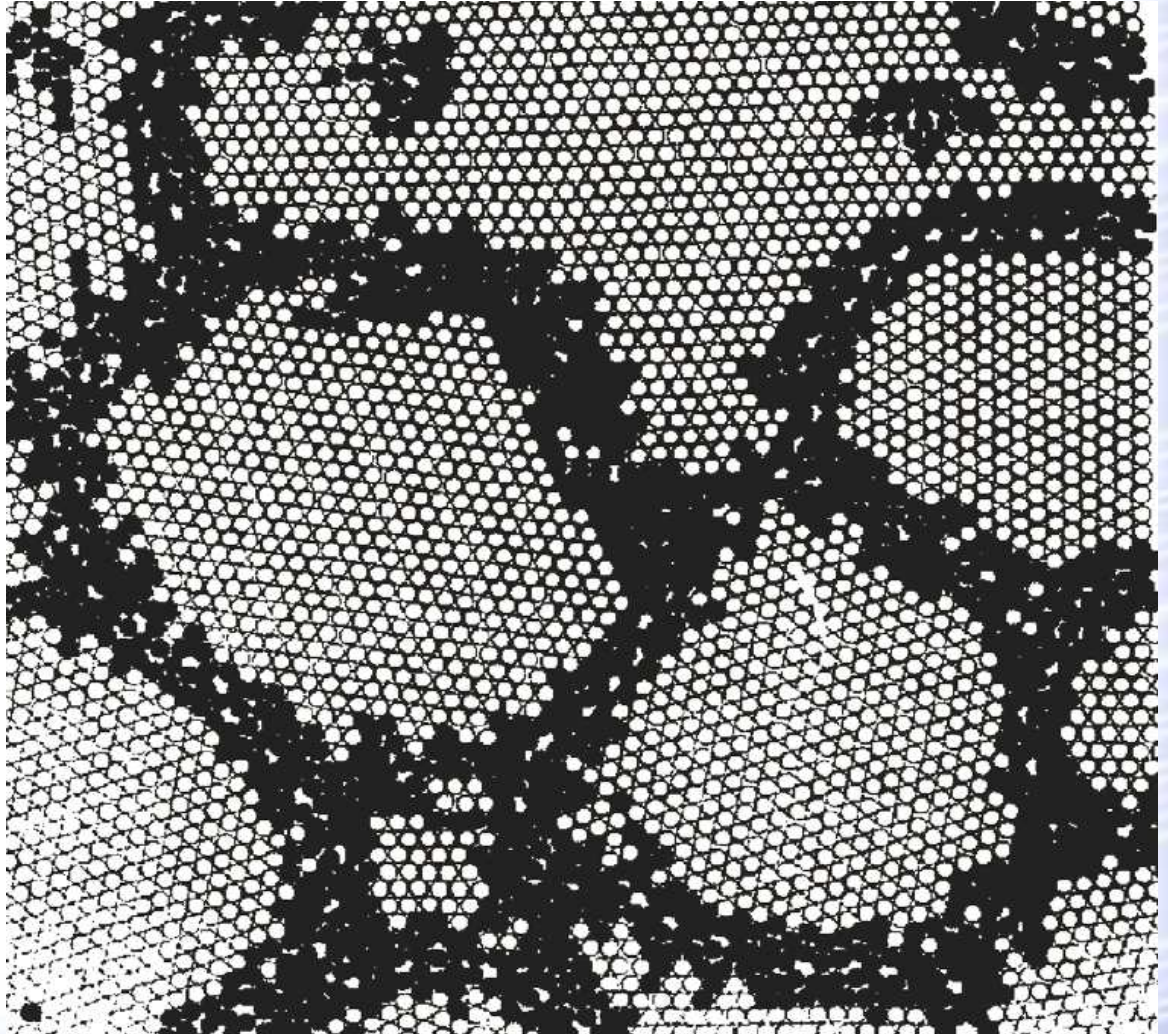
Dispersion hardening by composites - red optimum

Armour hardening by composites - blue optimum

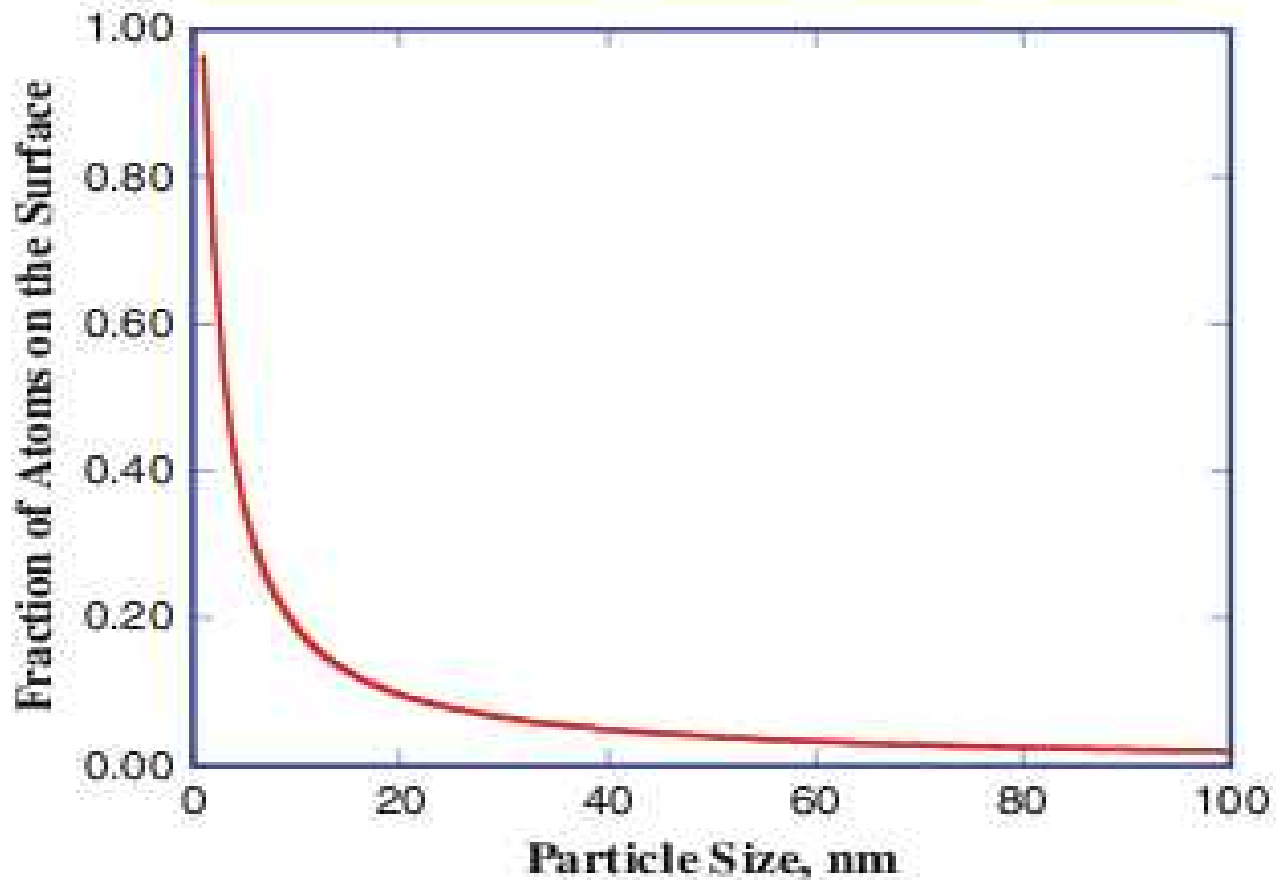


Nanoparticles

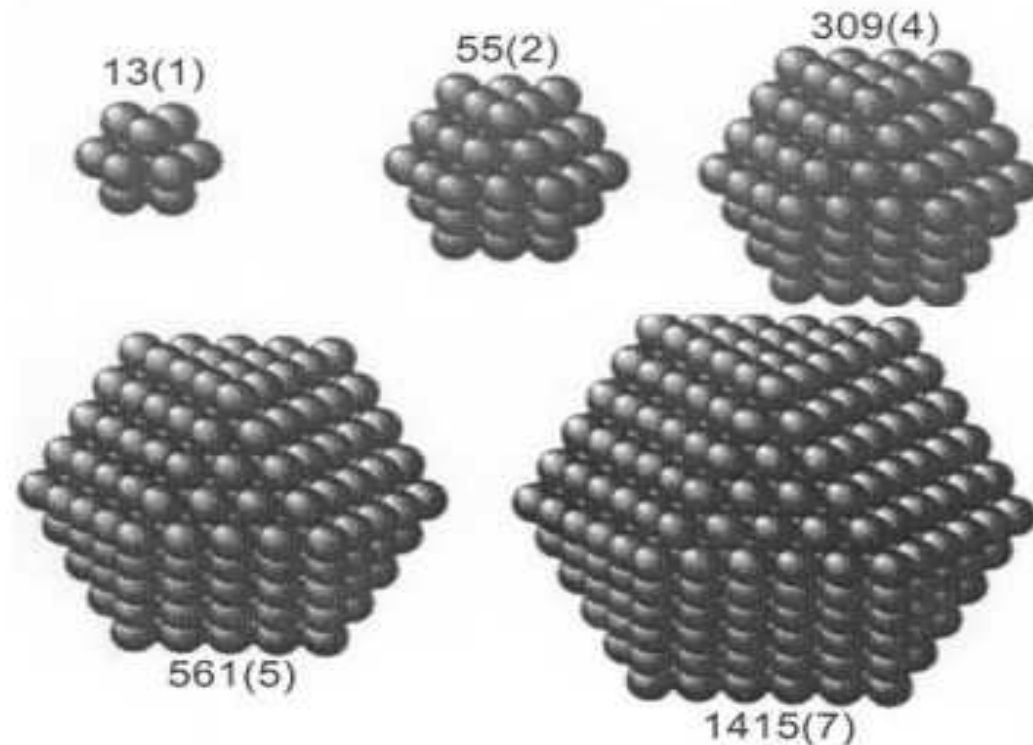
- Boundary layers :
 - more reactive
 - lower density
 - dispersion of interatomic distances



Fraction of surface atoms



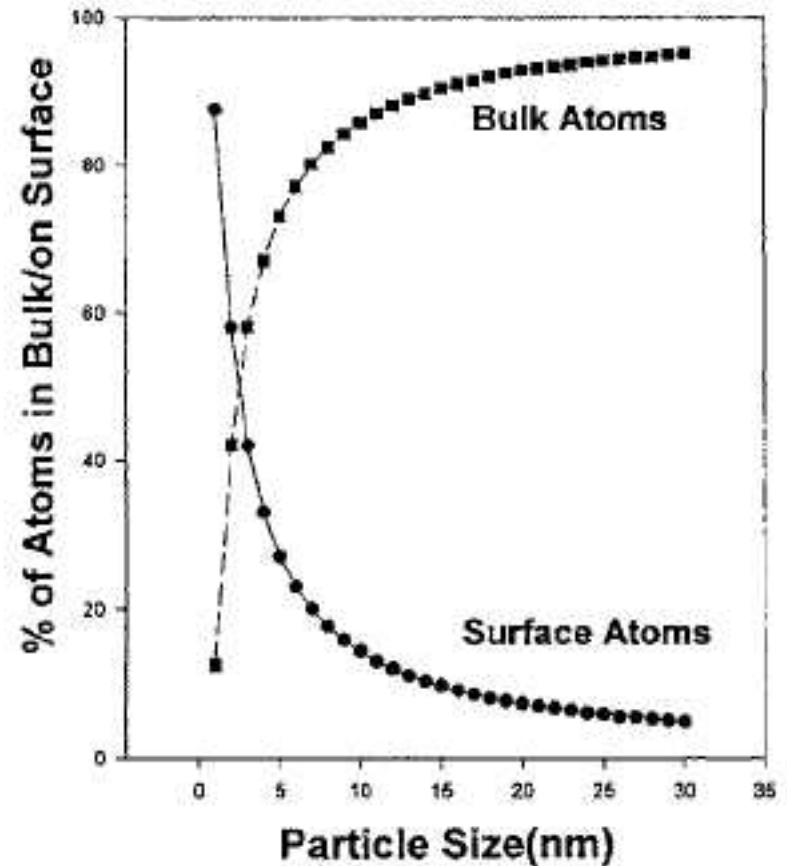
Nanocrystals - metal clusters



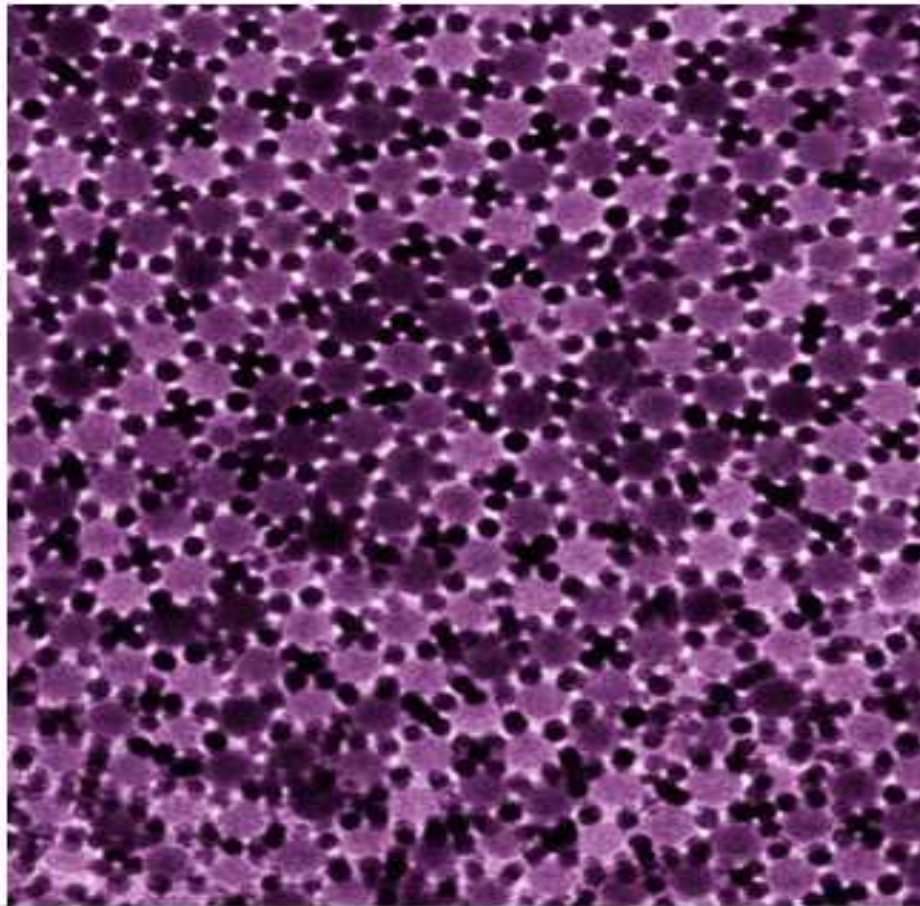
Metal nanocrystals in closed-shell configurations with a magic number of atoms. The number of shells is indicated in brackets.

Surface of metal clusters

Full-shell Clusters	Total Number of Atoms	Surface Atoms (%)
1 Shell	13	92
2 Shells	55	76
3 Shells	147	63
4 Shells	309	52
5 Shells	561	45
7 Shells	1415	35

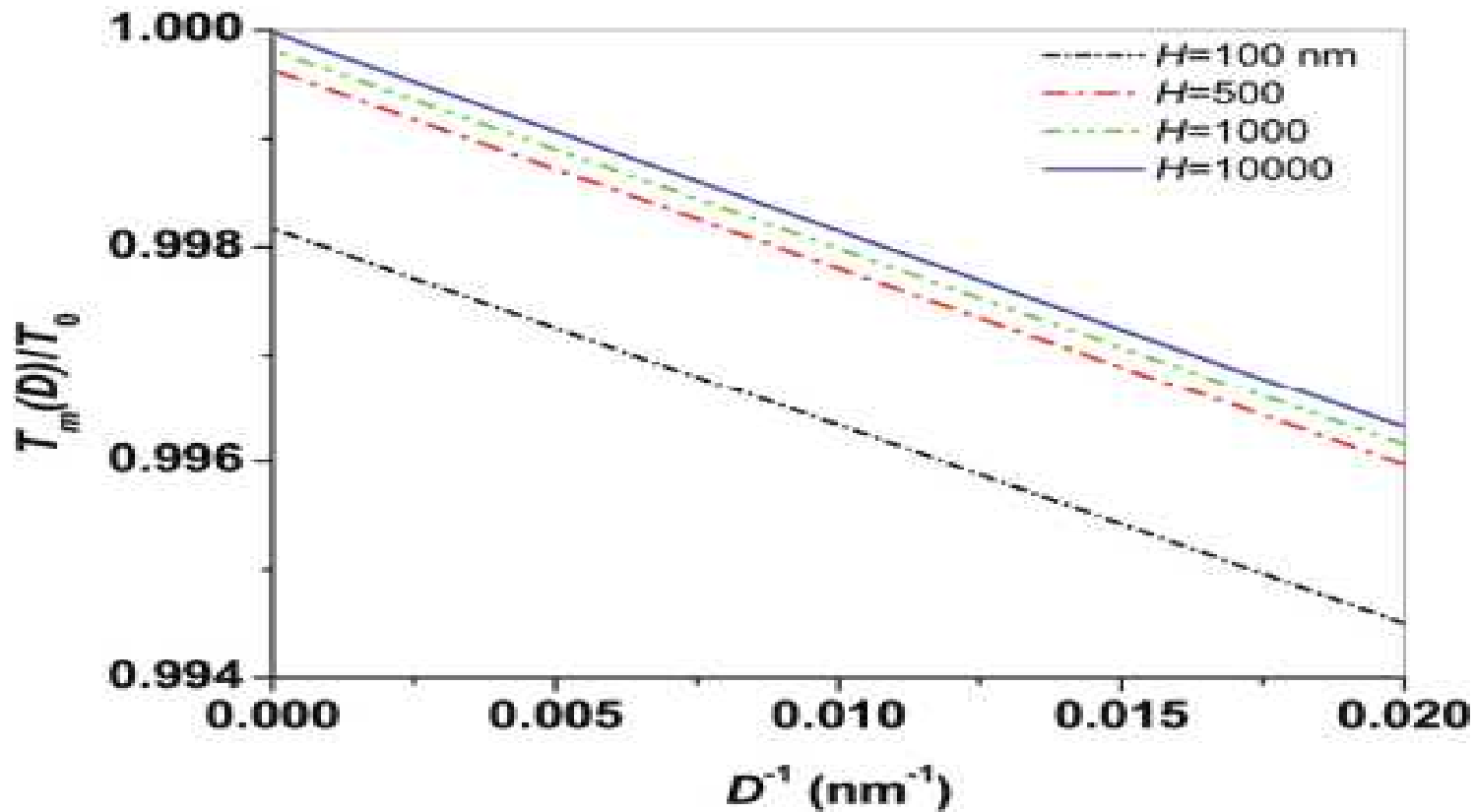


Quasicrystals from nanoparticles - coagulation



TEM showing the two-dimensional dodecagonal quasi-crystalline structure self-assembled from 5-nm Au and 13.4-nm Fe₃O₄ nanoparticles.

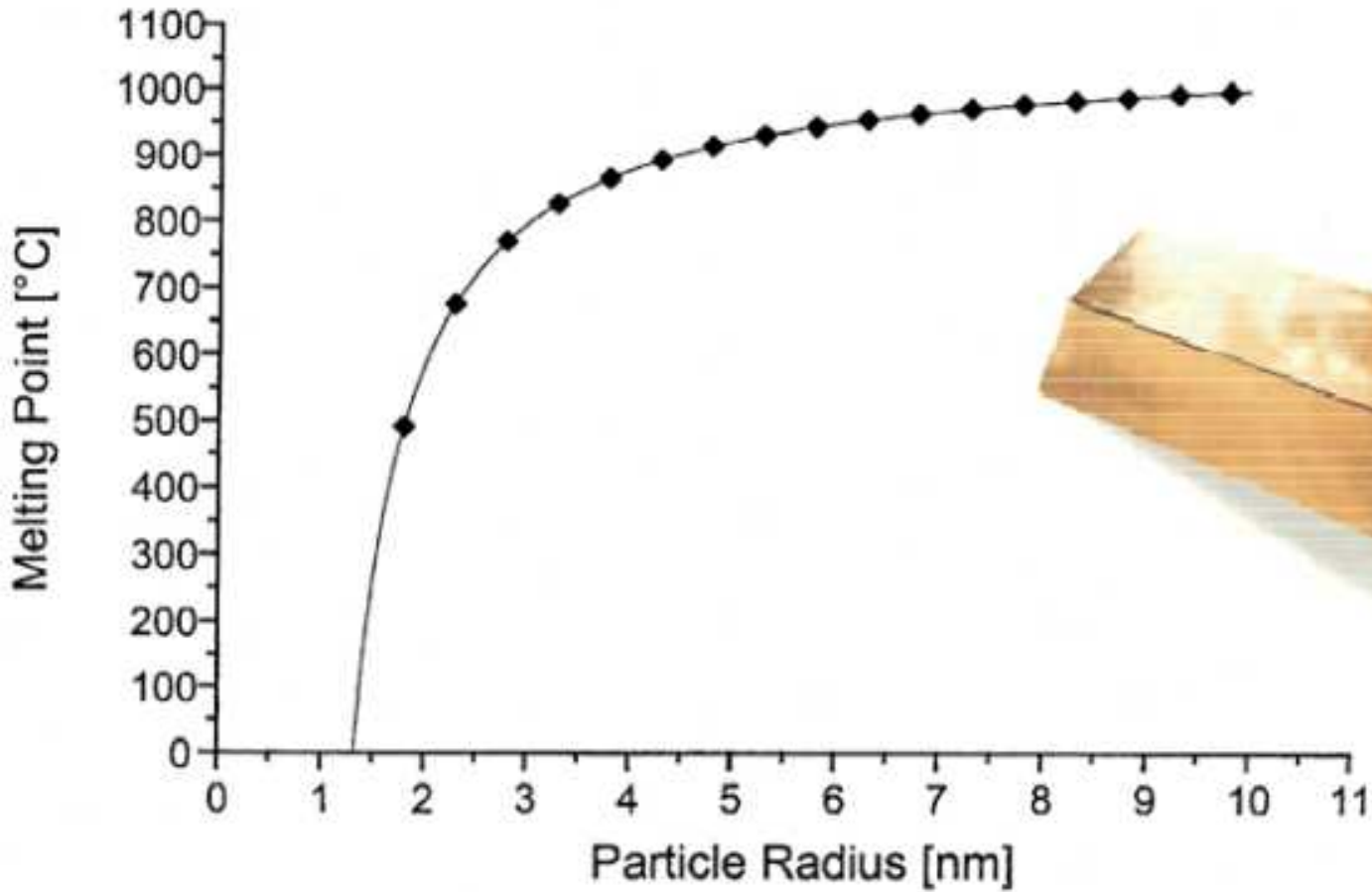
Dependence of melting point on particle size



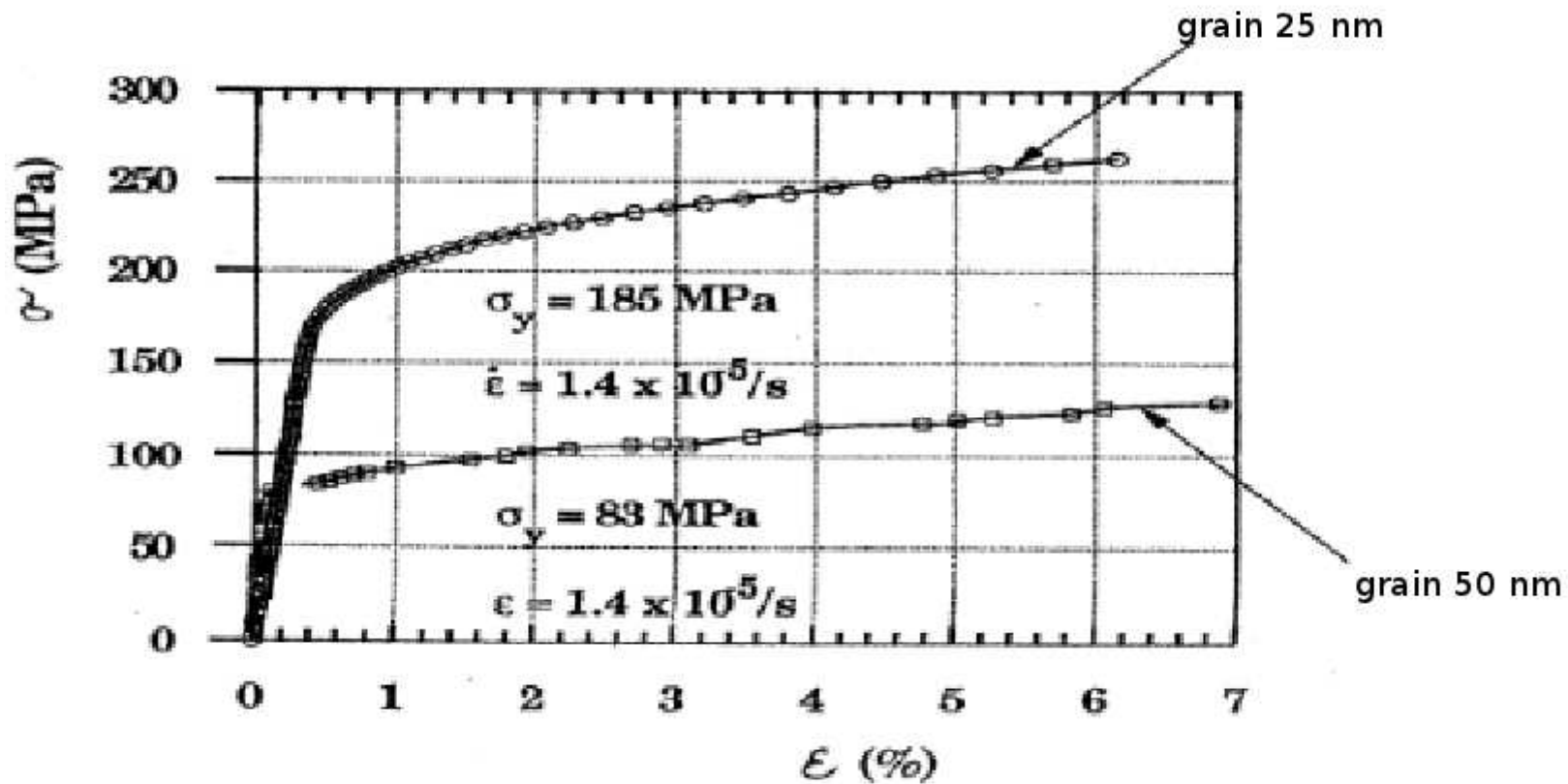
D ... edge of base, H ... high of prism. Thermodynamic model.

Experimental dependence

melting point of massive Aurum : 1064 °C



Influence of particle size on Ultimate Strength



Tensile test of Cuprum
Strength 2,3 x greater

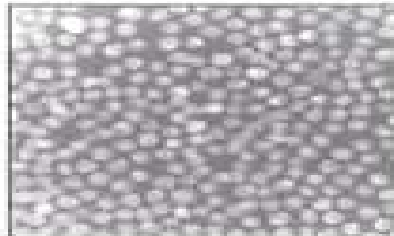
Nanoparticle colours

Gold particles in glass

Size*: 25 nm
Shape: sphere
Color reflected:

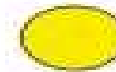


100 nanometers =
0.0001 millimeter



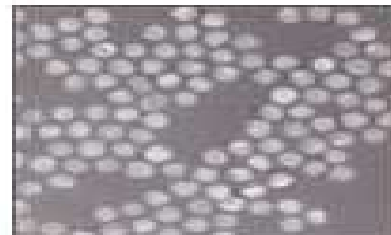
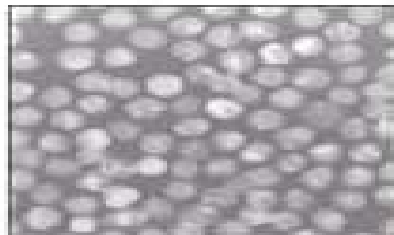
Silver particles in glass

Size*: 100 nm
Shape: sphere
Color reflected:



Had medieval artists been able to control the size and shape of the nanoparticles, they would have been able to use the two metals to produce other colors. Examples:

Size*: 50 nm
Shape: sphere
Color reflected:



Size*: 40 nm
Shape: sphere
Color reflected:



Size*: 100 nm
Shape: sphere
Color reflected:



Size*: 100 nm
Shape: prism
Color reflected:



Source: Dr. Chad A. Mirkin, Institute of Nanotechnology, Northwestern University

*Approximate

Zdroj obrázku: Institute of Nanotechnology, Northwestern University